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Zu Inhaltsverzeichnis

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Application of Self-Organizing Maps to the Maritime Environment

Victor J.A.S. Lobo
Portuguese Naval Academy, Alfeite, 2810-001 Almada, Portugal, vlobo@isegi.unl.pt

Abstract. Self-Organizing Maps (SOMs), or Kohonen networks, are widely used neural network architecture. This paper starts with a brief overview of how SOMs can be used in different types of problems. A simple and intuitive explanation of how a SOM is trained is provided, together with a formal explanation of the algorithm, and some of the more important parameters are discussed. Finally, an overview of different applications of SOMs in maritime problems is presented.

Keywords: Self-organizing maps; SOM; Kohonen networks

1 Introduction

Although the term “Self-Organizing Map” has been used to designate a number of different entities, it generally refers to Kohonen’s Self Organizing Map [1], or SOM for short. These maps are also referred to as “Kohonen Neural Networks” [2], “Topological Neural Networks” [3], “Self-organizing Feature Maps (SOFM),” or “Topology preserving feature maps” [1], or some variant of these names.

Professor Kohonen worked on auto-associative memory during the 1970s and early 1980s, and presented his SOM algorithm in 1982 [4]. However, it was not until the publication of the second edition of his book “Self-Organization and Associative Memory” in 1988 [5], and his paper named “The Neural Phonetic Typewriter” on IEEE Computer [5] that his
work became widely known. Since then, there have been many excellent papers and books on SOM, but his 2001 book [1] is generally regarded as the main reference on the subject. This book has had very flattering reviews, presenting a thorough covering of the mathematical background for SOM, its physiological interpretation, the basic SOM, developments, and applications.

Although Professor Kohonen has retired, his research group maintains a very good web-site at Helsinki’s Technical University at “http://www.cis.hut.fi/research.” That site contains public domain software, various manuals, papers, technical reports, and a very thorough and searchable list of papers dealing with SOM (available at “http://www.cis.hut.fi/research/som-bibl” and containing a total of 7,718 references in December 2008). The som_pak programs, that are available with source code, and the Somtoolbox for Matlab, are of particular interest to anyone wanting to experiment with SOM. We strongly recommend a visit to these sites.

Kohonen himself describes SOM as a “visualization and analysis tool for high dimensional data.” These are indeed the two most attractive characteristics of SOM, but, as we shall see, it can be used for many other applications.

1.1 What Can a SOM Do?

Despite the simplicity of the SOM algorithm, it can and has been used to perform many different tasks, the most common of which are:

1. **Clustering (k-means type clustering):** This is probably the most common application of SOM, albeit probably not the best. In this context, the SOM is used as an alternative to k-means clustering [6–8], i.e., given a fixed number $k$ of clusters, the SOM will partition the available data into $k$ different groups. As an example, we may want to divide customers into four different groups according to their characteristics, for marketing purposes. The main advantage of SOM in this case is that it is less prone to local minima than the traditional k-means clustering algorithm, and thus can act as a good initialization algorithm for that method. In fact, it can substitute k-means altogether, for as noted in [9], the final stages of the SOM training algorithm are exactly the same as the k-means algorithm. An extra bonus of the SOM algorithm is that the clusters obtained are topologically ordered, i.e., similar clusters are (usually) grouped together.
2. **Exploratory data analysis and visualization**: This is, arguably, the most important application of SOM. In this case, the SOM is used as a nonlinear projection algorithm, mapping $n$-dimensional data onto a one or two dimensional grid. The SOM can thus be an alternative to PCA projections, principal curves, or multidimensional scaling (MDS) algorithms such as Sammon mappings [10]. Different projection algorithms perform different trade-offs when mapping from high to low dimensions, since in all but the most trivial cases some information will be lost. The main advantage of projecting multidimensional data onto one or two dimensions is that we can easily visualize the data in these dimensions. From this visualization, we can identify outliers (data points that are far from other data), identify data that are similar to a given reference, or generally compare different data. If we project data onto one dimension, we may then plot histograms, and thus identify “natural” clusters of data. A similar result may be obtained with a technique closely related to SOM called U-Matrix [11] that can be extended to visualize what can loosely be interpreted as a two-dimensional histogram.

3. **Ordering of multidimensional data**: This type of application makes use of the topological ordering of the SOM to organize a given set of data vectors according to some criteria. As an example, a 1-dimensional SOM can be used to solve the well-known traveling salesman or related problems [12]. Another interesting use of this ordering capacity of a SOM is to create color palettes from pictures.

4. **Supervised data classification**: The SOM is not meant to be a classifier, and a related technique called linear vector quantization (LVQ) [1] is best suited for this task. However, just like the centroids obtained by a $k$-means algorithm, a SOM may also be used to supervise classification by labeling the neurons (or units) with the classes of the data that are mapped to it.

5. **Sampling**: The units of a SOM have a probability distribution that is a function of the probability distribution of the data used for training. Generally, the SOM will over-represent regions of the input space that have a low density, but that is frequently an advantage since it helps detect outliers and novel data patterns.

6. **Feature extraction**: Since the SOM performs a mapping from a high-dimensional space to a low dimensional one, it may be used for feature extraction. In the simple case, the new features are simply the coordinates of the mapped data point. This is one of the few cases where SOMs with a dimension greater than two are easy to use.

7. **Control and/or data sensitive processing**: A SOM can be used to select, based on available data, the best model, controller, or data...
processor for a given situation. The main idea behind this type of application is that instead of designing a rather complex controller, multiple simple controllers may be used, each one tuned to a particular type of situation. During the training of the SOM the input data are partitioned into various Voronoi regions, and each of these is used to train or define the parameters of a different controller.

8. Data interpolation: When using the SOM to interpolate data, the output space of the SOM will have the same dimension as the input space, but since the units are ordered on a regular grid, that grid provides a locally linear interpolator for the data.

Beyond these more typical applications of SOM, there have been many others, and a complete list is not practical or indeed interesting. An example of an unexpected application is the use of SOM to draw cartograms [13].

## 2 Basic Principles

A SOM is single layer neural network. The name neural network, or more correctly artificial neural network, is due to the historical fact that they were originally inspired by the way biological neurons were believed to work. Although this analogy is, generally speaking, still valid, developments in artificial neural networks and in our knowledge of how biological neurons actually work have led many researchers to refer to the basic computing units of artificial neural networks not as “neurons,” but as “units.” In this paper, to stress the difference between the mathematical model of a biological neuron and our computational units, we will follow the more recent conventions, and refer to them simply as “units.”

There are also many terms used to designate the data that are used to train the network, or later to use it. In this paper, we will follow the term most used in the pattern recognition community, which is simply “pattern” or “data pattern.” Different communities will call it “sample,” “instance,” “point,” or “entity.”

In a SOM, the units are set along an $n$-dimensional grid. In most applications, this grid is two-dimensional and rectangular, though many applications use hexagonal grids, and one, three, or more dimensional spaces. In this grid, we can define neighborhoods in what we call the output space, as opposed to the input space of the data patterns.

Each unit, being an input layer unit, has as many weights or coefficients as the input patterns, and can thus be regarded as a vector in the same space as the patterns. When we train or use a SOM with a given input pattern, we calculate the distance between that pattern and every unit in the
network. We then select the unit that is closest as the winning unit (or best matching unit – BMU), and say that the pattern is mapped onto that unit. If the SOM has been trained successfully, then patterns that are close in the input space will be mapped to units that are close (or the same) in the output space and, hopefully, vice-versa. Thus, SOM is “topology preserving” in the sense that (as far as possible) neighborhoods are preserved through the mapping process.

Generally, no matter how much we train the network, there will always be some difference between any given input pattern and the unit it is mapped to. This is a situation identical to vector quantization, where there is some difference between a pattern and its code-book vector representation. This difference is called quantization error, and is used as a measure of how well map units represent the input patterns.

We can look at a SOM as a “rubber surface” that is stretched and bent all over the input space, so as to be close to all the training points in that

Fig. 1 Basic SOM architecture. On the bottom, the input patterns are shown as a four-dimensional vector (left) or three-dimensional point (right). The units are also points in this input space. On the top, the grid of units is shown (left) together with a U-matrix coloring of a SOM.
Let us imagine a very simple example, where we have four clusters of three-dimensional training patterns, centered at four of the vertices of the unit cube: (0,0,0), (0,0,1), (1,1,0), and (1,1,1). If we trained a two-dimensional, four node map, we would expect to obtain units centered at those vertices. If we use a larger map, with 16 nodes, for example, we would expect to obtain a map where the units are grouped in clusters of four nodes on each of the vertices (see Fig. 2).

Before training, the units may be initialized randomly. During the first part of training, they are “spread out,” and pulled towards the general area (in the input space) where they will stay. This is usually called the unfolding phase of training. After this phase, the general shape of the network in the input space is defined, and we can then proceed to the fine tuning phase, where we will match the units as far as possible to the input patterns, thus decreasing the quantization error.

To visualize the training process, let us follow a two-dimensional to one-dimensional mapping presented in [1]. In this problem, two-dimensional data points are uniformly distributed in a triangle, and a one-dimensional...
SOM is trained with these patterns. Figure 4 represents the evolution of the units in the input space. As training proceeds, the line first unfolds (steps 1–100), and then fine-tunes itself to cover the input space.

3 Description of the Training Algorithm

3.1 The Algorithm

Let $x_k$ (with $k = 1$ to the number of training patterns $N$) be the $n$-dimensional training patterns. Let $w_{ij}$ be the unit in position $(i, j)$. Let $0 \leq \alpha \leq 1$ be the learning rate (sometimes referred to as $\eta$), and $h(w_{ij}, w_{mn}, r)$ be the neighborhood function (sometimes referred to as $\Lambda$ or $N_c$). This neighborhood function has values in $[0,1]$ and is high for units that are close in the output space, and small (or 0) for units far away. It is usual to select a function that is 1 if $w_{ij} = w_{nn}$, monotonically decreases as the distance in the grid between them increases up to a radius $r$ (called neighborhood radius) and is zero from there onwards. Let $w_{bmu}$ be the best matching unit for a given input pattern.

The algorithm for training the network is then:

For each input pattern $x_k$:

1. Calculate the distances between the pattern $x_k$ and all units $w_{ij}$:
   \[ d_{ij} = \|x_k - w_{ij}\| \]

2. Select the nearest unit $w_{ij}$ as best matching unit $w_{bmu} = w_{ij}$:
   \[ d_{ij} = \min(d_{mn}) \]

3. Update each unit $w_{ij}$ according to the rule $w_{ij} = w_{ij} + \alpha \cdot h(w_{bmu}, w_{ij}, r)$
   \[ \|x_k - w_{ij}\| \]

4. Repeat the process until a certain stopping criterion is met. Usually, the stopping criterion is a fixed number of iterations. To guarantee convergence and stability of the map, the learning rate $\alpha$ and neighborhood radius $r$ are decreased in each iteration, thus converging to zero.
The distance measure between the vectors is usually the Euclidean distance, but many others can and are used, such as norm-based Minkowski metrics, dot products, director cosines, Tanimoto measures, or Hausdorff distances.

### 3.2 Neighborhood Functions

The neighborhood function provides a bond between a unit and its neighbors, and is responsible for the topological ordering of the map. In fact, without this neighborhood function (or when its radius is zero), the SOM training algorithm is exactly the same as the incremental $k$-means algorithm [6]. The two most common neighborhood functions are the Gaussian and the square (or bubble) functions:

$$h_g(w_i, w_m, r) = \frac{1}{\sqrt{2\pi r^2}} e^{-\frac{(i-n)^2 + (j-m)^2}{2r^2}},$$

$$h_i(w_i, w_m, r) = \begin{cases} 1 & \text{if } (i-n)^2 + (j-m)^2 \leq r \\ 0 & \text{if } (i-n)^2 + (j-m)^2 > r. \end{cases}$$

In both cases, $r$ decreases to 0 or 1 during training. If $r \to 0$ the final quantization error will be minimized, but the topological ordering may be lost, since the algorithm is performing a $k$-means clustering. On the other hand, forcing $r \to 1$ will preserve the ordering of the units, but the quantization error will not be minimized. Moreover, in this case, there will be a border effect, by which units close to the border will be dragged to the center, and present higher quantization errors.

The algorithm is surprisingly robust to changes in the neighborhood function, and our experience is that it will usually converge to approximately the same final map, whatever our choice, providing the radius and learning rate decrease to 0. The Gaussian neighborhood tends to be more reliable (different initializations tend to converge to the same map), while the bubble neighborhood leads to smaller quantization errors, and is computationally much faster. A theoretic discussion of the effect of neighborhood functions (although only for the one-dimensional case) can be found in [17], and a less rigorous but more general one in [18].


3.3 Other Parameters and Training Options

As mentioned before, training is usually done in two phases: the unfolding phase, and the fine-tuning phase. The algorithm is exactly the same in both cases, but while in the first phase the neighborhood radius and learning rate have rather high values (to allow for a general orientation of the map), in the second phase they will have smaller values, to perform only fine adjustments on the unit’s positions. As a rule of thumb, the initial radius for the first phase should be roughly the length of the smaller side of the map, while for the second it should be the radius of the expected size of clusters in the output space.

The size of the map will depend a lot on the particular problem at hand and on the data available. If the SOM is to be used as an alternative to k-means, one unit per desired cluster should be used. For that type of application, a one-dimensional SOM will usually provide the best results [9]. For exploratory data analysis, a larger map should be used. These are sometimes called emergent-SOM or ESOM [19]. Depending on the amount and variability of available data, a rule of thumb could be to use one unit for each 4–20 or more data patterns, but in some cases one might use more units than data patterns (to obtain very clear cut U-Matrices).

3.4 U-Matrices

U-Matrices were introduced by Ultsch [11] and are one of the most popular and useful ways of visualizing clusters with a SOM. A U-Matrix is obtained by computing the distance in the input space of units that are neighbors in the output space. If these differences are small, it means that the units are close together, and thus there is a cluster of similar data in that region of the input space. On the other hand, if the distances are large, the units are far apart, and there isn’t much data in that region of the input space. The U-Matrix can thus be seen as a sort of extension of an inverted histogram for multidimensional data projected on a lower dimensional space: low values indicate large concentrations of data and high values indicate sparse regions. U-Matrices are usually presented as color-coded maps: white regions indicate low values (and thus clusters), while dark regions indicate separations between clusters.
Many different variants of the basic SOM algorithm have been proposed, and a complete review of these is beyond the scope of this paper. Some reviews of these variants have been published [20, 21], and we will overview some of them to show how the basic algorithm can be adapted to different problems.

The original SOM algorithm and most of its variants deal with vector data only. Some variants for non-vector data have also been proposed namely the dissimilarity SOM [22], the Kohonen multiple correspondence analysis and the Kohonen algorithm on disjunctive table [23]. For the simpler case of binary valued data, both the original algorithm using 0 and 1 as real numbers and binary variants of SOM produce good results [24, 25].

SOMs have frequently been used to analyze temporal data, such as EEG or Stock Exchange data. In most cases, time can be imbedded into the data vector, and a standard SOM algorithm is used, treating that vector as a simple input pattern. More interesting uses of SOM have been made by changing the learning rule or by changing the topology or structure of the network so as to explicitly take time into consideration. In the former case, the learning rule may, for example, consider only the neighbors of the last BMU as candidates for the next input pattern, or separate the time variable from the rest when computing the similarity. As for changes in topology and structure, some approaches use hierarchical SOMs with different time frames, or include time delay memories in the units. A review of the different ways in which this has been done, together with a proposal for a taxonomy of temporal SOMs, is available in [26].

Geographical information science problems also have a special variable (special location) that should, like time, be treated in a different way. To this end a variant called GeoSOM has been developed [21, 27, 28].

Hierarchical SOMs [29, 30] combine several SOMs to process data at a low level, and then use their outputs as inputs to a high level SOM that fuses the results.

In some applications, the notion of output grid is substituted by a more general graph, such as happens in the minimum spanning tree SOM [20], tree-structured SOM [29], or growing cells [31, 32]. The links and concept of output space may even disappear, as happens in the neural gas model [15, 33, 34].

Another important type of variants on the basic SOM algorithm are those that try and overcome the theoretical obstacles raised by the fact that the SOM does not minimize a global energy function. One solution is to
change the learning rule slightly, as was done in [35]. Another solution is to use a variation of Gaussian mixture models to derive a topologically ordered map, as is done with generative topographic mapping [36]. However, despite the theoretical soundness of these methods, they do not provide significantly better results and are computationally more complex than the original algorithm.

5 Applications in Maritime Environment

Given the wide range of capabilities of the SOM there have been many applications of this technique on maritime problems.

SOMs have been used quite frequently to cluster and classify satellite images [3, 37–41]. In most cases, the SOM is basically used as a classifier, and each pixel of the satellite image forms a data pattern. When analyzing satellite images, the ground truth (i.e., the real class of a given pixel) is usually established by an expert, and is rather slow, expensive, and prone to errors. Therefore not many classified pixels are available. One advantage of the SOM in this case is that it may be trained with all the data, including nonclassified pixels, and then labeled with only the classified ones. This labeling may then be extended to other units that belong to the same cluster, improving the classification capabilities of the system. Very similar approaches have been made with data that combine satellite images with other data [42], data obtained by radar [43], data obtained by meteorological stations [44], airborne lasers [45], or even data obtained by simulators. The common factor in all these cases is that a two-dimensional map with pixels that are multidimensional vectors is presented to a SOM for clustering and classification. Let us look at one of these in a little more detail, and then overview the problems where these approaches were successfully applied.

One application of SOM to satellite images, that concerns reflectance spectra of ocean waters, is presented in [3]. In this case, a 20 × 20 unit probabilistic SOM (or more precisely PSOM) is trained with 43,000 six-dimensional vectors. Each of these corresponds to sampled pixels of a satellite image with five preprocessed frequency bands, and an extra value corresponding to the spatial standard deviation of one of those measurements. A human expert will then label some of the pixels, and these are used to label the SOM units, either directly or indirectly, after these are clustered with a hierarchical clustering algorithm. The authors point out that the method used provides a good overall classification of the data, in part due to the fact that the probabilistic nature of PSOM allows for a
confidence level to be assigned to each classification. The PSOM is also considered useful by showing that a lot of resources are dedicated to separating clouds from other pixels, thus leading to the suggestion that the images be preprocessed to remove these clouds. The author’s main interest is in the characterization of Sahara dust, clouds, and other aerosols present over the ocean, and they do not go into great detail on the parameterization of the PSOM. It could be argued that a nonsquare map would lead to a better stabilization of the training process, and that the use of a U-Matrix would help define larger clusters (instead of using hierarchical clustering), but the authors did not follow that path.

The SOM has been used in a similar way (i.e., for clustering and classifying data contained in two-dimensional maps or images), in many applications of environmental science, climatology, geology, and oceanography. These include analyzing sea surface temperature [46–49], plankton [50, 51], ocean current patterns [43, 52], estuary and basin dynamics [53], sediment structure [54], atmospheric pressure [55, 56], wind patterns [39], storm systems [41], the El Niño weather conditions [42], clouds [57], ice [53, 58, 59], rainfall [44, 60, 61], oil spills [45], the influence of ocean conditions in droughts [62], and the relationship between sardine abundance and upwelling phenomena [40].

Data concerning fisheries were analyzed in different perspectives using a SOM in [63]. The use of SOM in this case clearly shows the existence of well-defined changes in fisheries over time, and relationships between different species.

A more creative use of SOM is shown in [64], where the SOM is used to segment maps of the seafloor obtained with multibeam sonars. The segmented data is then classified with specialized classifiers for each segment. The SOM is thus used to preprocess the data so that multiple simpler or more precise classifiers can be used to obtain the desired results.

Although classical harmonical methods can provide good sea level predictions in most cases, those predictions can have rather large errors in basins, estuaries, or regions where weather conditions have a large influence. In those cases, SOMs have been used to predict sea levels with greater accuracy in [65].

Following an approach common in several problems in robotics [66], the SOM has been used to control an underwater autonomous vehicle (AUV) [67–69]. The basic idea in this type of application is that the SOM receives the sensor inputs, and based on that chooses a unit that will provide the guidance for the AUV. The main advantage of the SOM in this case is that each of the units has a quite simple control law (as opposed to a complicated nonlinear controller), and the topological ordering of the SOM makes it relatively robust to noise in the inputs.
With the increase in maritime traffic, the consequences of accidents, and the availability of vessel traffic systems (VTS), the automatic detection of anomalous behaviors of ships became a pressing problem. This problem was addressed, in [70], where track data (heading, speed, etc.) from navy exercises was used to train a SOM. Clusters were then identified on that SOM, and both suspicious behavior clusters and outliers were flagged as potential threats. The same problem was tackled in a similar way in [71]. In this case, the emphasis is more on visualization of the data, and on estimating the probability of a given situation occurring in the dataset.

Also related to ship trajectories, SOMs have been used to plan patrol trajectories of naval vessels in [72]. The approach followed was basically the one used to solve the traveling salesman problem with a SOM (e.g., [12]). In this case, the geographical locations of “incidents” (accidents and illegal fishing) were used as training patterns, and the trajectory obtained tries to maximize the probability of passing in the area where there were “incidents” in the past.

In underwater acoustics, SOMs have been used extensively to analyze passive sonar recordings [73–76]. Although ship noise or transient recognition is basically a supervised task, it is very important to detect novelties, and to relate those novelties to known causes. The SOM can provide this by using large maps which will have many unlabeled units. Additionally, it provides an easy to use and understand interface for the operators.

Also concerning fluids, although not directly applied to the maritime environment, an interesting use of SOM is given in [77, 78] for analyzing movement in fluids by tracking particles in suspension. The idea is to use successive images of the fluid for training a map, and then infer the movement by observing how the units change from one step to the next.

6 Conclusions

An introduction to how a SOM works and how it can be used has been presented. Despite its simplicity, the SOM can be used for a wide variety of applications. Some of its shortcomings were also pointed out, as well as the main issues that must be taken into consideration when using them.

An overview of applications in the marine environment has been given, showing that it has successfully been used in many real maritime problems. I believe that its use in this field is still at a preliminary stage, and more and more powerful uses will be given to SOM. It is frequently used simply for $k$-means type clustering and supervised classification. While those types of applications are useful, I think that the greatest potential of
SOM is its ability to project and visualize multidimensional data. Many authors have criticized clustering through visualization as too subjective for engineering purposes. I would argue that clustering is intrinsically a subjective problem, and that the human eye and judgment are the best tools available for that task. The computer algorithms should only present the data in a suitable way, which is exactly what a SOM does. I also believe that there is still a lot of potential for using SOM in nonlinear control and routing or piping problems aboard ships. As SOMs become more mainstream, and software for their use becomes more widespread, they will probably be used in creative ways in even more problems.

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